

### **Homework 3**

**P2.3.5** Determine  $V_O$  by redrawing the ladder network of Figure 2.3.5 as a cascade of three voltage dividers.

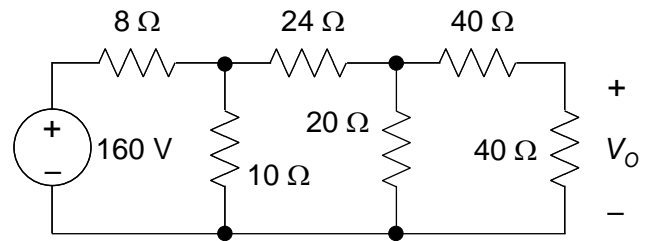


Figure P2.3.5

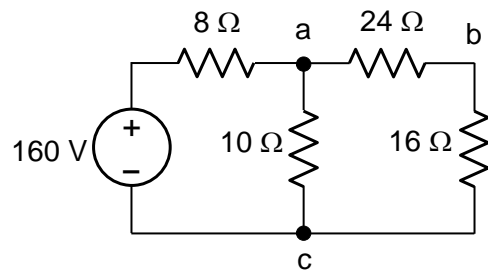
### **Solution P2.3.5**

$$20 \parallel (40 + 40) = 16 \, \Omega; \quad 10 \parallel (24 + 16) = 8 \, \Omega;$$

$$\text{hence } V_{ac} = 160 \times \frac{8}{16} = 80 \, \text{V},$$

$$V_{bc} = 80 \times \frac{16}{24 + 16} = 32 \, \text{V},$$

$$V_O = 32 \times \frac{40}{80} = 16 \, \text{V}.$$



**P2.3.6** Determine  $I_o$  by redrawing the ladder network of Figure 2.3.6 as a cascade of three current dividers.

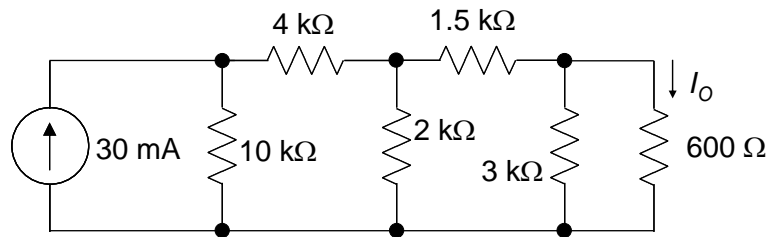


Figure P2.3.6

**Solution P2.3.6**

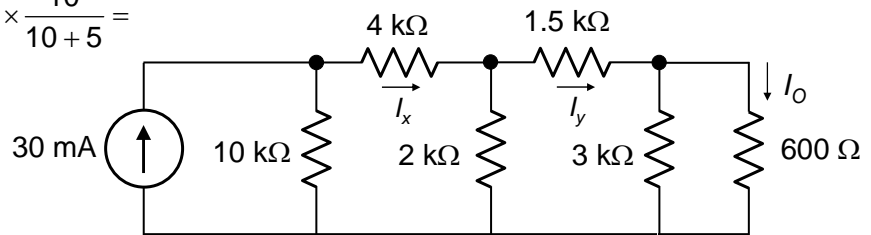
$$0.6 \parallel 3 = 0.5 \text{ k}\Omega; (1.5 + 5) = 2 \text{ k}\Omega;$$

$$\text{from current division: } I_x = 30 \times \frac{10}{10 + 5} =$$

$$20 \text{ mA};$$

$$I_y = 20 \times \frac{2}{2 + 2} = 10 \text{ mA};$$

$$I_o = 10 \times \frac{3}{3.6} = \frac{25}{3} \text{ m A.}$$



**P2.4.1** Determine  $V_O$  in Figure P2.4.1 using two methods: (a) applying KCL at node a and invoking KVL and Ohm's law; and (b) transforming the voltage source to an equivalent current source that is combined with the 4 mA source.

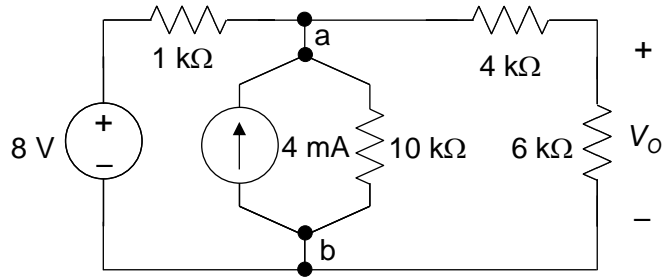


Figure P2.4.1

**Solution P2.4.1**

(a)  $V_{ab} = \frac{10}{6} V_O$ ;

current flowing away from node a:  $\frac{V_O}{6} + \frac{10}{6 \times 10} V_O = \frac{V_O}{3} \text{ mA}$ ;

current flowing toward a:  $4 + \frac{8 - \frac{10V_O}{6}}{1} = 12 - \frac{5V_O}{3}$ .

Hence,  $12 - \frac{5V_O}{3} = \frac{V_O}{3}$ , which gives  $V_O = 6 \text{ V}$ .

(b) Voltage source in series with 1 kΩ is transformed to 8 mA source in parallel with 1 kΩ; total current is 12 mA;

total resistance is  $1 || 10 || 10 = \frac{5}{6} \text{ k}\Omega$ ;

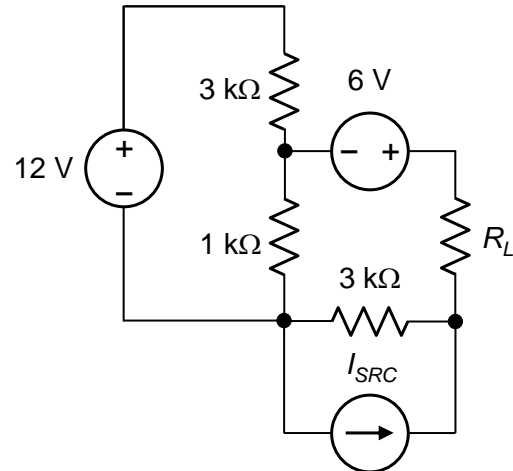
$V_{ab} = 12 \times \frac{5}{6} = 10 \text{ V}$ ;  $V_O = 10 \times \frac{6}{10} = 6 \text{ V}$ .

**P2.4.3** Determine  $I_{SRC}$  in Figure P2.4.3 so that no current flows in  $R_L$ .

**Solution P2.4.3**

When no current flows in  $R_L$ , the voltage across the  $1\text{ k}\Omega$  resistor is  $12 \times \frac{1}{4} = 3\text{ V}$ , and  $I_{SRC}$  flows in the  $3\text{ k}\Omega$  resistor.

The voltage across this resistor is then  $3 + 6 = 9\text{ V}$ , so that  $3I_{SRC} = 9$ , and  $I_{SRC} = 3\text{ mA}$ .



**P2.4.4** Determine  $V_O$  in Figure P2.4.4.

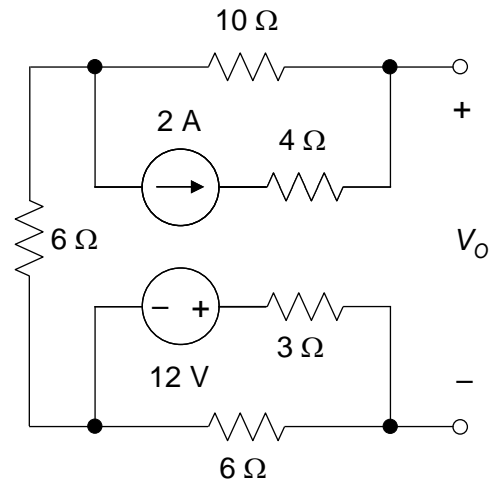


Figure P2.4.4

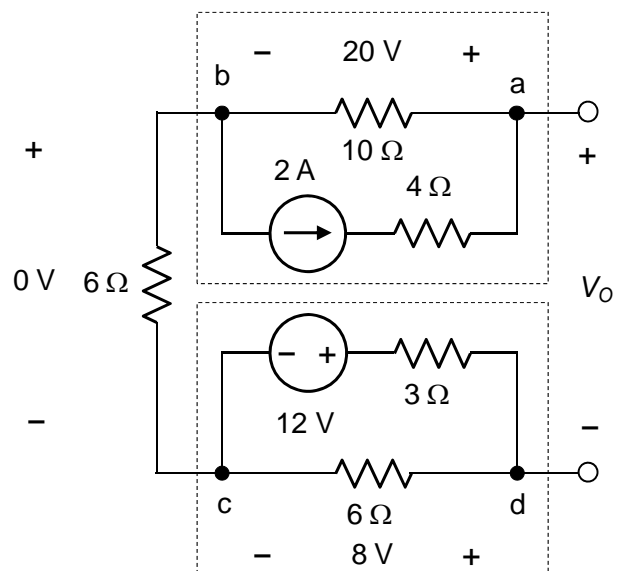
**Solution P2.4.4**

From KCL applied to the dashed rectangles, the current in the  $6\ \Omega$  resistor is zero.

Hence,  $V_{ab} = 10 \times 2 = 20\text{ V}$ ;

$$V_{dc} = 12 \times \frac{6}{9} = 8\text{ V};$$

Applying KVL starting at node d and going CW:  
 $-8 + 0 + 20 - V_O = 0$ , which gives  $V_O = 12\text{ V}$ .



**P2.4.5** Determine  $V_O$  in Figure P2.4.5, assuming  $\alpha = 3$ .

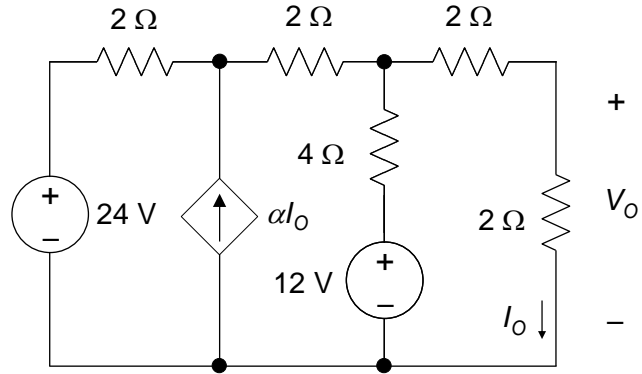


Figure P2.4.5

**Solution P2.4.5**

Since  $I_O = \frac{V_O}{2}$ , the dependent

current source becomes  $\frac{\alpha V_O}{2}$ .

The 24 V source in series with 2 Ω is transformed to a 12 A source in parallel with 2 Ω.

Similarly, the 12 V source in

series with 4 Ω is transformed to a 3 A source in parallel with 4 Ω.

This resistor is then combined with the 4 Ω to give a resistance of 2 Ω in parallel with the 3A source.

The voltage of the upper RHS node is  $2V_O$ .

KCL for the node on the LHS gives:  $12 + \frac{\alpha V_O}{2} = I_x + \frac{V_a}{2}$ , where  $\frac{V_a}{2}$  is the current that flows away from the node through the 2 Ω resistor.

KCL at the RHS node gives:  $3 + I_x = \frac{2V_O}{2}$ .

Substituting  $I_x = \frac{V_a - 2V_O}{2}$  gives two equations in the two unknowns  $V_a$  and  $V_O$ :

$$V_a - \left(1 + \frac{\alpha}{2}\right)V_O = 12, \text{ and } V_a - 4V_O = -6.$$

$$\text{Eliminating } V_a \text{ gives: } V_O = \frac{18}{3 - \alpha/2}.$$

If  $\alpha = 3$ ,  $V_O = 12$  V. Note that if  $\alpha = 6$ ,  $V_O$  is indeterminate.

**P2.4.12** Find  $V_{SRC}$ ,  $V_x$ ,  $V_y$ ,  $I_{SRC}$ , and the current in each resistor in Figure. P2.4.12.

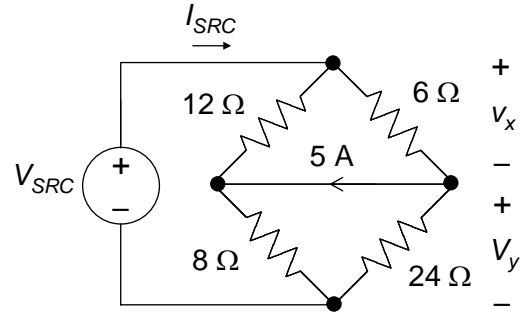


Figure P2.4.12

**Solution P2.4.12**

Let the current in the  $6\ \Omega$  resistor be  $I_1$ ;

from KCL at node b, the current in the  $24\ \Omega$  resistor is  $(I_1 - 5)$  A.

Similarly, if the current in the  $12\ \Omega$  resistor is  $I_2$ , then from KCL at node d, the current in the  $8\ \Omega$  resistor is  $(I_2 + 5)$ .

From KVL around mesh abd:  $6I_1 = 12I_2$ ;

from KVL around mesh bcd:  $24(I_1 - 5) = 8(I_2 + 5)$ .

Solving for  $I_1$  and  $I_2$  gives:  $I_1 = 8$  A and  $I_2 = 4$  A.

From KCL at node a:  $I_{SRC} = I_1 + I_2 = 12$  A;

$V_x = 6I_1 = 48$  V;

$V_y = 24(I_1 - 5) = 72$  V;

hence,  $V_{SRC} = V_x + V_y = 120$  V.

It follows that  $I_{6\Omega} = 8$  A,  $I_{12\Omega} = 4$  A,  $I_{24\Omega} = 3$  A, and  $I_{8\Omega} = 9$  A.

